

## Lista 1 – TCM

Prof. Rafael Gabler Gontijo

Os exercícios abaixo foram extraídos do livro: “Fundamentals of Heat and Mass Transfer”, Sexta edição, dos autores Incropera, DeWitt, Bergman e Lavine.

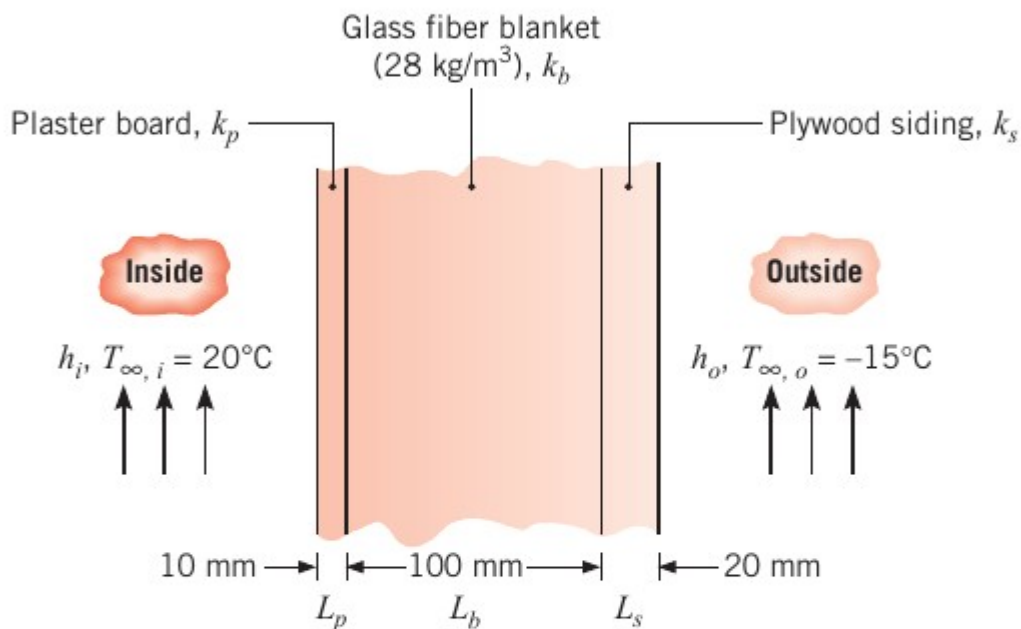
### Exercício 1

**3.10** The *wind chill*, which is experienced on a cold, windy day, is related to increased heat transfer from exposed human skin to the surrounding atmosphere. Consider a layer of fatty tissue that is 3 mm thick and whose interior surface is maintained at a temperature of  $36^{\circ}\text{C}$ . On a calm day the convection heat transfer coefficient at the outer surface is  $25 \text{ W/m}^2 \cdot \text{K}$ , but with 30 km/h winds it reaches  $65 \text{ W/m}^2 \cdot \text{K}$ . In both cases the ambient air temperature is  $-15^{\circ}\text{C}$ .

- (a) What is the ratio of the heat loss per unit area from the skin for the calm day to that for the windy day?
- (b) What will be the skin outer surface temperature for the calm day? For the windy day?
- (c) What temperature would the air have to assume on the calm day to produce the same heat loss occurring with the air temperature at  $-15^{\circ}\text{C}$  on the windy day?

## Exercício 2

**3.13** A house has a composite wall of wood, fiberglass insulation, and plaster board, as indicated in the sketch. On a cold winter day, the convection heat transfer coefficients are  $h_o = 60 \text{ W/m}^2 \cdot \text{K}$  and  $h_i = 30 \text{ W/m}^2 \cdot \text{K}$ . The total wall surface area is  $350 \text{ m}^2$ .



- Determine a symbolic expression for the total thermal resistance of the wall, including inside and outside convection effects for the prescribed conditions.
- Determine the total heat loss through the wall.
- If the wind were blowing violently, raising  $h_o$  to  $300 \text{ W/m}^2 \cdot \text{K}$ , determine the percentage increase in the heat loss.
- What is the controlling resistance that determines the amount of heat flow through the wall?

### Exercício 3

- 3.14** Consider the composite wall of Problem 3.13 under conditions for which the inside air is still characterized by  $T_{\infty,i} = 20^\circ\text{C}$  and  $h_i = 30 \text{ W/m}^2 \cdot \text{K}$ . However, use the more realistic conditions for which the outside air is characterized by a diurnal (time) varying temperature of the form

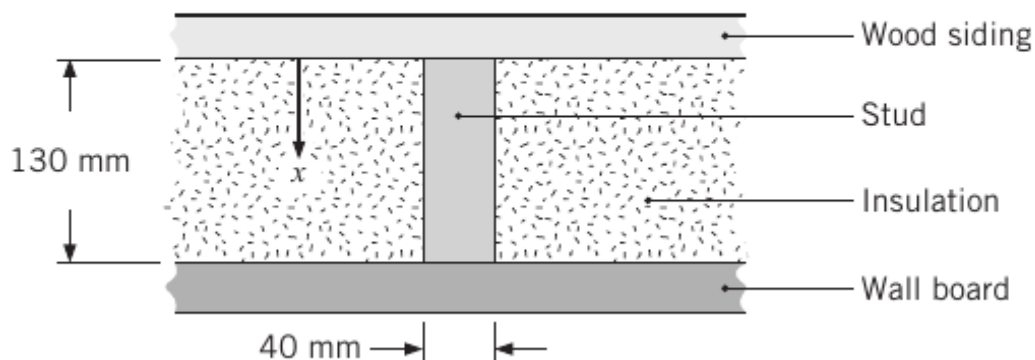
$$T_{\infty,o}(\text{K}) = 273 + 5 \sin\left(\frac{2\pi}{24}t\right) \quad 0 \leq t \leq 12 \text{ h}$$

$$T_{\infty,o}(\text{K}) = 273 + 11 \sin\left(\frac{2\pi}{24}t\right) \quad 12 \leq t \leq 24 \text{ h}$$

with  $h_o = 60 \text{ W/m}^2 \cdot \text{K}$ . Assuming quasi-steady conditions for which changes in energy storage within the wall may be neglected, estimate the daily heat loss through the wall if its total surface area is  $200 \text{ m}^2$ .

### Exercício 4

- 3.15** Consider a composite wall that includes an 8-mm-thick hardwood siding, 40-mm by 130-mm hardwood studs on 0.65-m centers with glass fiber insulation (paper faced,  $28 \text{ kg/m}^3$ ), and a 12-mm layer of gypsum (vermiculite) wall board.



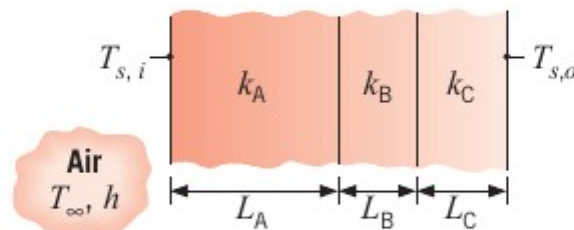
What is the thermal resistance associated with a wall that is 2.5 m high by 6.5 m wide (having 10 studs, each 2.5 m high)? Assume surfaces normal to the  $x$ -direction are isothermal.

## Exercício 5

- 3.16 Work Problem 3.15 assuming surfaces parallel to the  $x$ -direction are adiabatic.

## Exercício 6

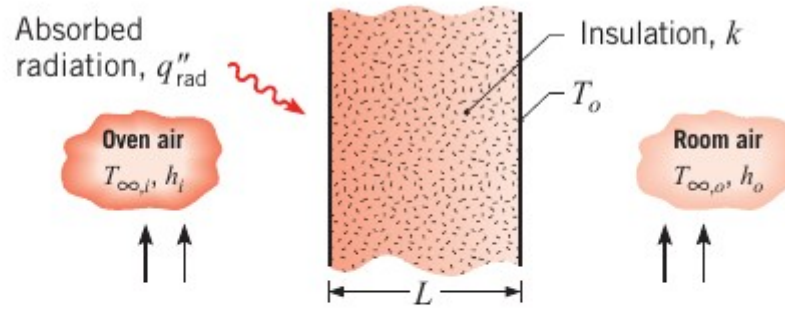
- 3.18 The composite wall of an oven consists of three materials, two of which are of known thermal conductivity,  $k_A = 20 \text{ W/m}\cdot\text{K}$  and  $k_C = 50 \text{ W/m}\cdot\text{K}$ , and known thickness,  $L_A = 0.30 \text{ m}$  and  $L_C = 0.15 \text{ m}$ . The third material, B, which is sandwiched between materials A and C, is of known thickness,  $L_B = 0.15 \text{ m}$ , but unknown thermal conductivity  $k_B$ .



Under steady-state operating conditions, measurements reveal an outer surface temperature of  $T_{s,o} = 20^\circ\text{C}$ , an inner surface temperature of  $T_{s,i} = 600^\circ\text{C}$ , and an oven air temperature of  $T_{\infty} = 800^\circ\text{C}$ . The inside convection coefficient  $h$  is known to be  $25 \text{ W/m}^2\cdot\text{K}$ . What is the value of  $k_B$ ?

## Exercício 7

- 3.19 The wall of a drying oven is constructed by sandwiching an insulation material of thermal conductivity  $k = 0.05 \text{ W/m}\cdot\text{K}$  between thin metal sheets. The oven air is at  $T_{\infty,i} = 300^\circ\text{C}$ , and the corresponding convection coefficient is  $h_i = 30 \text{ W/m}^2\cdot\text{K}$ . The inner wall surface absorbs a radiant flux of  $q''_{\text{rad}} = 100 \text{ W/m}^2$  from hotter objects within the oven. The room air is at  $T_{\infty,o} = 25^\circ\text{C}$ , and the overall coefficient for convection and radiation from the outer surface is  $h_o = 10 \text{ W/m}^2\cdot\text{K}$ .



- Draw the thermal circuit for the wall and label all temperatures, heat rates, and thermal resistances.
- What insulation thickness  $L$  is required to maintain the outer wall surface at a *safe-to-touch* temperature of  $T_o = 40^\circ\text{C}$ ?

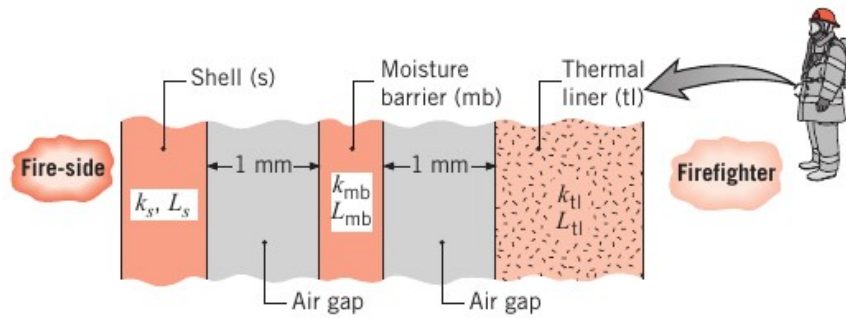
### Exercício 8

- 3.20** The  $t = 4\text{-mm}$ -thick glass windows of an automobile have a surface area of  $A = 2.6\text{ m}^2$ . The outside temperature is  $T_{\infty,o} = 32^\circ\text{C}$  while the passenger compartment is maintained at  $T_{\infty,i} = 22^\circ\text{C}$ . The convection heat transfer coefficient on the exterior window surface is  $h_o = 90\text{ W/m}^2\cdot\text{K}$ . Determine the heat gain through the windows when the interior convection heat transfer coefficient is  $h_i = 15\text{ W/m}^2\cdot\text{K}$ . By controlling the air-flow in the passenger compartment the interior heat transfer coefficient can be reduced to  $h_i = 5\text{ W/m}^2\cdot\text{K}$  without sacrificing passenger comfort. Determine the heat gain through the window for the reduced inside heat transfer coefficient.

### Exercício 9

- 3.24** A firefighter's protective clothing, referred to as a *turnout coat*, is typically constructed as an ensemble of three layers separated by air gaps, as shown schematically.





Representative dimensions and thermal conductivities for the layers are as follows.

Layer	Thickness (mm)	$k$ (W/m · K)
Shell (s)	0.8	0.047
Moisture barrier (mb)	0.55	0.012
Thermal liner (tl)	3.5	0.038

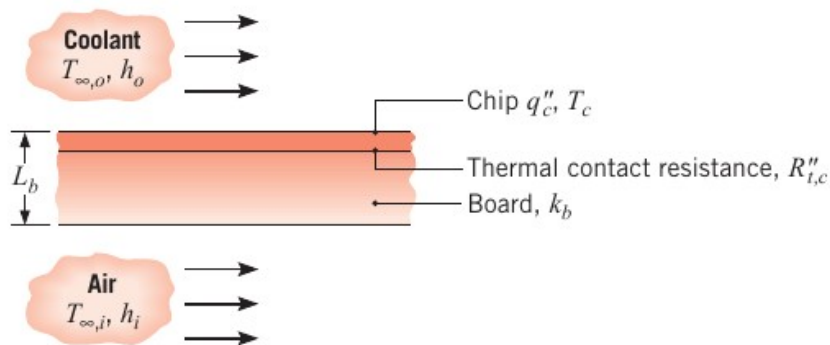
The air gaps between the layers are 1 mm thick, and heat is transferred by conduction and radiation exchange through the stagnant air. The linearized radiation coefficient for a gap may be approximated as,  $h_{\text{rad}} = \sigma(T_1 + T_2)(T_1^2 + T_2^2) \approx 4\sigma T_{\text{avg}}^3$ , where  $T_{\text{avg}}$  represents the average temperature of the surfaces comprising the gap, and the radiation flux across the gap may be expressed as  $q''_{\text{rad}} = h_{\text{rad}}(T_1 - T_2)$ .

- Represent the turnout coat by a thermal circuit, labeling all the thermal resistances. Calculate and tabulate the thermal resistances per unit area ( $\text{m}^2 \cdot \text{K}/\text{W}$ ) for each of the layers, as well as for the conduction and radiation processes in the gaps. Assume that a value of  $T_{\text{avg}} = 470 \text{ K}$  may be used to approximate the radiation resistance of both gaps. Comment on the relative magnitudes of the resistances.
- For a *pre-flash-over* fire environment in which firefighters often work, the typical radiant heat flux on the fire-side of the turnout coat is  $0.25 \text{ W}/\text{cm}^2$ .

What is the outer surface temperature of the turnout coat if the inner surface temperature is  $66^\circ\text{C}$ , a condition that would result in burn injury?

## Exercício 10

- 3.27 Approximately  $10^6$  discrete electrical components can be placed on a single integrated circuit (chip), with electrical heat dissipation as high as  $30,000 \text{ W/m}^2$ . The chip, which is very thin, is exposed to a dielectric liquid at its outer surface, with  $h_o = 1000 \text{ W/m}^2 \cdot \text{K}$  and  $T_{\infty,o} = 20^\circ\text{C}$ , and is joined to a circuit board at its inner surface. The thermal contact resistance between the chip and the board is  $10^{-4} \text{ m}^2 \cdot \text{K/W}$ , and the board thickness and thermal conductivity are  $L_b = 5 \text{ mm}$  and  $k_b = 1 \text{ W/m} \cdot \text{K}$ , respectively. The other surface of the board is exposed to ambient air for which  $h_i = 40 \text{ W/m}^2 \cdot \text{K}$  and  $T_{\infty,i} = 20^\circ\text{C}$ .



- (a) Sketch the equivalent thermal circuit corresponding to steady-state conditions. In variable form, label appropriate resistances, temperatures, and heat fluxes.
- (b) Under steady-state conditions for which the chip heat dissipation is  $q_c'' = 30,000 \text{ W/m}^2$ , what is the chip temperature?